

DESIGN AND ESTIMATED
WEIGHT OF A CANTILEVER BRIDGE

BY

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1914




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The design and estimated
weight of a cantilever

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THE DESIGN AND ESTIMATED WEIGHT OF A
CANTILEVER BRIDGE
A THESIS
PRESENTED BY
LEONARD ZEMAN & OTTO SIEDENSTRANG
TO THE
PRESIDENT AND FACULTY
OF
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FOR THE DEGREE OF
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HAVING COMPLETED THE PRESCRIBED COURSE OF STUDY IN
CIVIL ENGINEERING
- 1914 -

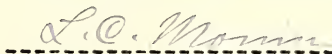
Approved.



Professor of Civil Engineering



Dean of Engineering Studies.



Dean of Cultural Studies.

PREFACE.

To demonstrate the fact, that the principles involved in analyzing a Cantilever Bridge are of a most elementary character, a complete set of values for stresses in the members of such a structure has been made. The "Method of Coefficients", which considers a load of unity concentrated at each panel point, was the plan adopted for the work. Since the analytical and graphical determination for stresses are self-explanatory, little explanation for the theory employed has been offered.

L.Z.

O.S.

June, '14

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on
THE DESIGN AND ESTIMATED WEIGHT OF A
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A BRIEF OUTLINE.

A) INTRODUCTION.

- a) The Idea of the Cantilever Bridge.
- b) Classification.
- c) Historical Notes.

B) DETERMINATION OF THE COEFFICIENTS FOR THE MEMBERS.

- a) Stresses due to DL & LL after bridge is finally up.
 - 1) Anchor Span, Cant. Span and Suspended Span.
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 - 1) Anchor, Cant., & Sus. Spans.
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- b) By Ketchums " " "
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D) COMPLETE DESIGN OF A FLOOR SYSTEM.

- a) Design of Stringers, Fl. Beams, etc.
- b) Determination of maximum shears.

E) TABULATION OF COEFFICIENTS AND STRESSES.



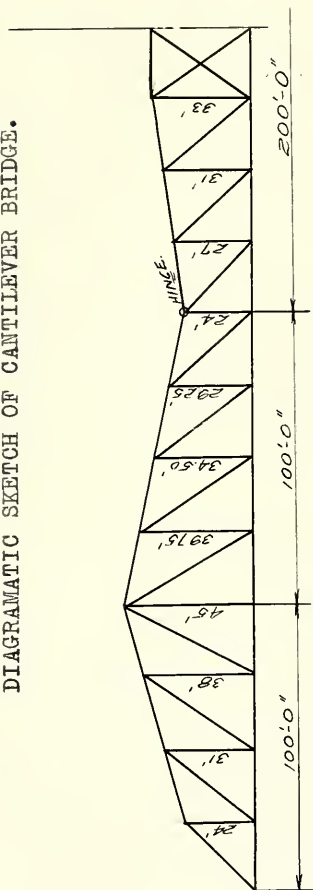
F) DESIGN OF SECTIONS AND ESTIMATION OF WEIGHTS.

- a) In suspended span.
- b) In cantilever arm.
- c) In anchor arm.

G) CONCLUDING REMARKS.



DIAGRAMATIC SKETCH OF CANTILEVER BRIDGE.



- (1) Anchor Span = 4 Panels @ 25'-0" = 100'-0"
 - (2) Cantilever Span = 4 Panels @ 25'-0" = 100'-0"
 - (3) Suspended Span = 8 Panels @ 25'-0" = 200'-0"
- Total length = 2 x (1) + 2 x (2) + (3) = 600'-0"

(Sketch #1)

INTRODUCTION.

Cantilever Bridges.

The Idea of the Cantilever Bridge:- The idea was first developed in the attempt to avoid the disadvantages of continuity. In a continuous bridge a slight elevation or depression of one support causes great changes in reactions and stresses. If, however, the chords be cut near the inflection points for full load, the inflection points for partial loads will occur there also, and thus the reactions will be statically determinate.

Classification:- A cantilever structure may be built as a deck or through bridge. Generally they have three spans; a simple style being the one considered in this thesis. Here the truss is supported at the piers upon a single pin. Then there is the cantilever structure which has two points of support at the pier. In this case there are no diagonals in the panel over the pier, this is to avoid the continuity

that would otherwise exist.

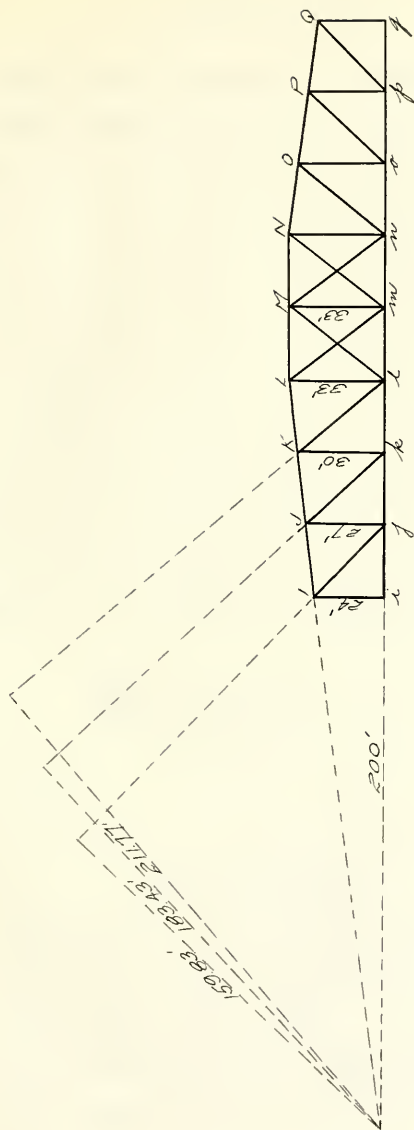
In either of these forms a load between the piers causes a negative reaction at the support, and this the greater the shorter the length of the shore span. To balance the negative reaction which may be caused by the live load, it is necessary that the truss be anchored at the abutment. The end span is hence called an anchor span or anchor arm. Thus for the bridge chosen for this Thesis a_e is the anchor span. The cantilever and suspended spans are respectively e_i and i_z . The suspended truss which connects the ends of the two cantilever arms is merely a simple truss supported at its ends. It is noted then, that it receives no stresses except those due to the loads upon its own floor, such being transmitted to the ends of the cantilever arms exactly as if these ends were abutments.

*Historical Notes:- The idea of building out cantilever beams from opposite shores of a stream and then bridging the interval between them by a

simple beam is an old one. An ancient structure of this kind in Japan is described in Von Nost-rand's Magazine for January, 1886, and one in Thibet of 112ft. in length is illustrated in THOMAS POPE'S Treatise on Bridge Architecture, published in New York 1811. This curious book of POPE is largely devoted to a design of his own, called the "flying pendant lever bridge" which was to be built out from the opposite shores until the cantilever arms met at the middle, these arms being anchored by huge abutments. With such a structure he proposed to bridge the Hudson river at New York, the span being about 3000 feet. His scheme met with little encouragement, and it was indeed an impractical one.

* From Merriam and Jacoby on ROOFS & BRIDGES.

DIAGRAMATIC SKETCH OF SUSPENDED SPAN.



(Sketch #2)

SUSPENDED SPAN

Dead Load Stresses:- The suspended span of this cantilever bridge consists of eight panels at 25'-0", totaling 200'-0". As indicated in the diagram of the preceding page there is a rise of 3'-0" in the upper chord of each panel, barring the middle ones which have parallel chords.

Consider a panel load of one kip concentrated at each panel point. Reaction = 4Kips. Then let y equal the distance to the intersection of the upper and lower chord from point i. $y = 24 \times 25 + 3 = 200'-0"$

$$\begin{aligned}\text{Tan. } \alpha &= 1.2 & \alpha &= 6^\circ - 51' \\ \text{Cos. } \alpha &= .99286 \\ \text{Sec. } \alpha &= 1.00719\end{aligned}$$

$$ij=0$$

$$Aa=-3.5$$

-Chord Stresses.-

$$IJ=-(3.5 \times 25) + (27 \times .9929) = -3.26$$

$$JK=-(3.5 \times 50) + 25 + (30 \times .9929) = -5.04$$

$$jk= 3.5 \times 25 + 30 = 3.24$$

$$KL=-(3.5 \times 75) + 50 + 25 + (33 \times .9929) = -5.73$$

$$kl= 3.5 \times 50 - 25 + 30 = 5.0$$

$$LM = -(3.5 \times 100) + (75 + 50 + 25) + 33 = -6.06$$

$$lm = (3.5 \times 75) - (50 + 25)$$

Diagonals.

$$\begin{aligned} \text{Tan. Iji} &= 24 + 25 = .96 & \text{Iji} &= 43^\circ - 50' \\ \text{Sin. Iji} &= 0.69256 \end{aligned}$$

$$\begin{aligned} \text{Tan. Jkj} &= 27 + 25 = 1.08 & \text{Jkj} &= 47^\circ - 12' \\ \text{Sin. Jkj} &= 0.73373 \end{aligned}$$

$$\begin{aligned} \text{Tan. Klk} &= 30 + 25 = 1.20 & \text{Klk} &= 50^\circ - 12' \\ \text{Sin. Klk} &= 0.76828 \end{aligned}$$

$$\begin{aligned} \text{Tan. Lml} &= 33 + 25 = 1.32 & \text{Lml} &= 52^\circ - 51' \\ \text{Cos. Lml} &= 0.6039 \\ \text{Sec. Lml} &= 1.65589 \end{aligned}$$

$$\begin{aligned} \text{Sec. lLm} &= 1.25462 & \text{lLm} &= 37^\circ - 09' \\ \text{Cos. lLm} &= 0.79706 \end{aligned}$$

$$Ij = 3.5 \times 200 + 155.83 = 4.5$$

$$Jk = (3.5 \times 200) - 225 + 183.43 = 2.59$$

$$Kl = (3.5 \times 200) - (250 + 225) + 211.28 = 1.064$$

$$Lm = .5 + 0.797 = 0.628$$

Posts.

$$Ii = -3.5$$

$$Jj = -(3.5 \times 200) + 225 + 225 = -2.11$$

$$Kk = -(3.5 \times 200) + 250 + 225 + 250 = -0.90$$

$$Ll = -(3.5 \times 200) + (275 + 250 + 225) + 275 = 1.82$$

$$Ee = 0$$

Live Load Stresses:- The live load chord stresses are the same as the dead load chord stresses.

* * * * *

Diagonals.

Load advancing from right.

$$Ij = 28 \times 200 + 8 \times 155.83 = 4.50 \text{ (Load up to j)}$$

$$Jk = 21 \times 200 + 8 \times 183.43 = 2.86 \text{ (Load up to k)}$$

$$Kl = 15 \times 200 + 8 \times 211.27 = 1.78 \text{ (Load up to l)}$$

$$Lm = 10 + 8 \times 0.797 = 1.57 \text{ (Load up to m)}$$

$$Mn = 6 + 8 \times 0.797 = 0.94 \text{ (Load up to n)}$$

Posts.

$$Jj = -21 \times 200 + 225 \times 8 = -2.33 \text{ (Load up to k)}$$

$$Kk = -15 \times 200 + 250 \times 8 = -1.50 \text{ (Load up to l)}$$

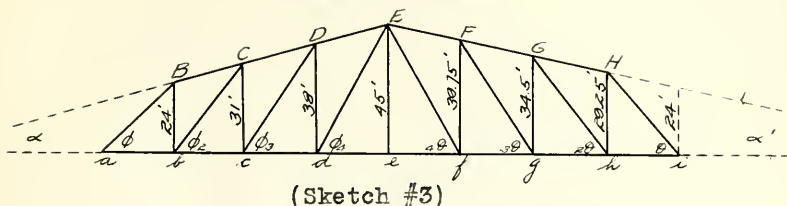
$$Ll = -10 \times 200 + 275 \times 8 = -0.91 \text{ (Load up to m)}$$

$$Mm \text{ by inspection} = .75 \text{ (Load up to n)}$$

For simplicity we submit the following.

Load up to:-	j	R= 28+8
	k	R= 21+8
	l	R= 15+8
	m	R= 10+8
	n	R= 6+8

ANCHOR SPAN
&
CANTILEVER ARM.



Considering the above figure, we have a panel length of 25'-0". The pier is located at e. The upper chord rises 7'-0" for all panels between B & E and 5'-3" for all panels between H & E .

The intersection of chords from a =

$$(24 + 27)25 - 25 = 60.7 \text{ Feet.}$$

The intersection of chords from i =

$$(24 + 5.25)25 = 114.29 \text{ Feet.}$$

$$\begin{aligned} \tan. \alpha &= 24 + 85.7 = .28 & \alpha &= 15^\circ - 39' \\ \cos. \alpha &= .96293 \end{aligned}$$

$$\begin{aligned} \tan. \alpha &= 24 + 114.29 = .21 & \alpha &= 11^\circ - 52' \\ \cos. \alpha &= .97863 \end{aligned}$$

$$\begin{aligned} \tan. \phi &= 24 + 25 = .96 & \phi &= 43^\circ - 50' \\ \cos. \phi &= .72136 \\ \sin. \phi &= .69256 \end{aligned}$$

$$\begin{aligned} \tan. \theta &= 29.25 + 25 = 1.17 & \theta &= 49^\circ - 29' \\ \cos. \theta &= .64967 \\ \sin. \theta &= .76022 \end{aligned}$$

Reaction at i = 4.5

CANTILEVER ARM.

Upper and Lower Chord Stresses.

$$H_1 = 4.5 + 0.76022 = 5.92$$

$$h_1 = -(4.5 \times 25) + 29.25 = -3.85$$

$$GH = 4.5 \times 25 + 29.25 \times .97863 = 3.92$$

$$hg = -(4.5 \times 50 - 25 \div 34.5 = -7.25$$

$$FG = 4.5 \times 50 + 25 + 34.5 \times .97863 = 7.4$$

$$fg = -(4.5 \times 75) - 25 - 50 + 39.75 = -10.4$$

$$EF = 4.5 \times 75 + 25 + 50 + 75 + 39.75 \times .97863 = 10.63$$

$$ef = -(4.5 \times 100) - 25 - 50 - 75 + 45 = -13.33$$

$$\begin{array}{ccccc} * & * & * & * & * \end{array}$$

Posts.

$$H_h = -(4.5 \times 114.29) + 139.29 = -3.695$$

$$G_g = -(4.5 \times 114.29) - 139.29 + 164.29 = 3.995$$

$$F_f = -(4.5 \times 114.29) - 139.29 - 164.29 + 189.29$$

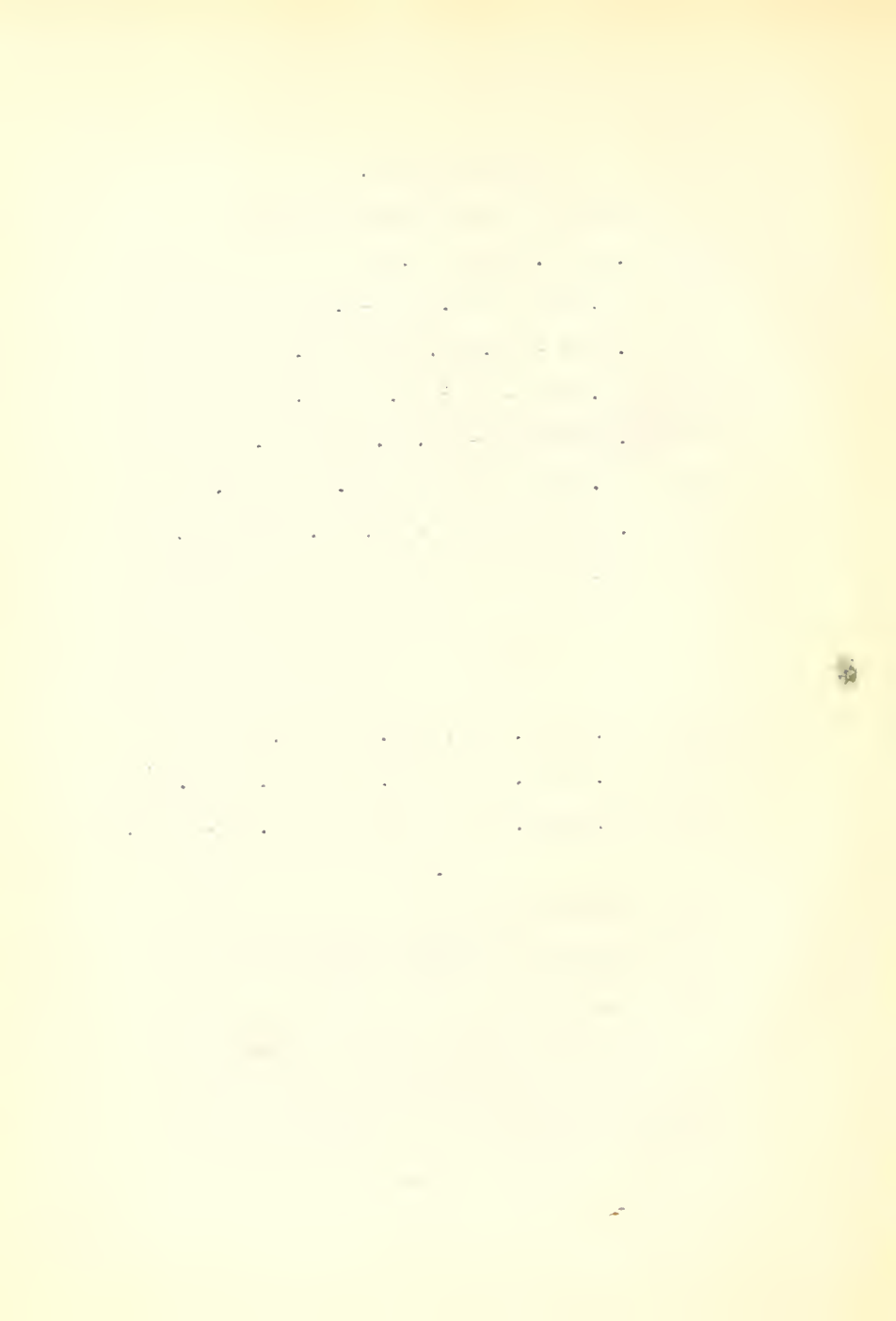
$$= 4.32$$

$$E_e = \text{Reaction at pier} =$$

$$(100 + 200 + 200 + 100 + 100 + 200) + 50 \text{ minus one}$$

$$\text{panel load} = 15$$

The terms of the above equations are merely substitutes for those in Merriam & Jacoby's formula.



Diagonals.

$$\begin{aligned}\text{Tan. } \theta &= 29.25 \div 25 = 1.17 & \theta &= 49^\circ - 29' \\ \text{Sin. } \theta &= .76022\end{aligned}$$

$$\begin{aligned}\text{Tan. } \theta_2 &= 34.5 \div 25 = 1.38 & \theta_2 &= 54^\circ - 4' \\ \text{Sin. } \theta_2 &= .80970\end{aligned}$$

$$\begin{aligned}\text{Tan. } \theta_3 &= 39.75 \div 25 = 1.59 & \theta_3 &= 57^\circ - 50' \\ \text{Sin. } \theta_3 &= .8465)\end{aligned}$$

$$\begin{aligned}\text{Tan. } \theta_4 &= 45.00 \div 25 = 1.8 & \theta_4 &= 60^\circ - 57' \\ \text{Sin. } \theta_4 &= .87420\end{aligned}$$

$$\text{Lever arm of H1} = 114.29 \times .76022 = 87.00'$$

$$\text{Gh} = 139.29 \times .80970 = 112.75'$$

$$\text{Fg} = 164.29 \times .8465) = 139.00'$$

$$\text{Ef} = 189.29 \times .87420 = 165.30'$$

The stresses then for the diagonals are viz:-

$$\text{H1} = 4.5 \times 114.29 \div 87 = 5.92$$

$$\text{Gh} = 4.5 \times 114.29 \div 139.29 \div 112.75 = 5.84$$

$$\begin{aligned}\text{Fg} &= 4.5 \times 114.29 \div 139.29 \div 164.29 \div 139 \\ &= 5.88\end{aligned}$$

$$\text{Ef} = 5.88 \div (189.29 \div 165.3) = 6.09$$

Thus far, all stresses have been obtained by the method of moments. In order to obtain accuracy, however, many of the stresses have been checked by the method of sections and by isolation of joints.

*** ANCHOR SPAN. ***

At the abutment end of the anchor span
 we have a negative reaction which is equal
 to $R = 100 - (100 + 100 \times 200 + 100) + 50$ minus
 .5 panel load = 4.5

Chord Stresses

$$ab = -4.5 \times 25 + 24 = -4.69$$

$$BC = 4.5 \times 25 + 24 \times .963 = 4.87$$

$$bc = -4.5 \times 50 - 25 + 31 = -8.06$$

$$CD = 8.06 + .963 = 8.38$$

$$cd = -4.5 \times 75 - 25 - 50 + 38 = -10.86$$

$$DE = 10.86 + .963 = 11.29$$

$$de = -4.5 - 25 - 50 - 75 + 45 = -13.32$$

Posts in Anchor Span.

$$Bb = -4.5 \times 60.7 + 85.7 = -3.185$$

$$Cc = -4.5 \times 60.7 - 25 + 110.7 = -2.7$$

$$Dd = -4.5 \times 60.7 - 25 - 50 + 135.7 = -2.57$$

Diagonals.

$$\begin{aligned}\text{Tan. } \phi_2 &= 31 + 25 = 1.24 & \phi_2 &= 51^\circ - 7' \\ \text{Sin. } \phi_2 &= .77843\end{aligned}$$

$$\begin{aligned}\text{Tan. } \phi_3 &= 38 + 25 = 1.52 & \phi_3 &= 56^\circ - 40' \\ \text{Sin. } \phi_3 &= .83549\end{aligned}$$

$$\begin{aligned}\text{Tan. } \phi_4 &= 45 + 25 = 1.80 & \phi_4 &= 60^\circ - 57' \\ \text{Sin. } \phi_4 &= .87420\end{aligned}$$

$$\text{Lever arm of Cb} = 85.7 \times .77843 = 66.8'$$

$$\text{Dc} = 110.7 \times .83549 = 92.5'$$

$$\text{Ed} = 135.7 \times .87420 = 118.5'$$

Stresses.

$$\text{aB} = 4.5 + .69256 = 6.5 \quad \text{Sin.} = .69252$$

$$\text{Cb} = 4.5 \times 60 + 25 + 66.8 = 4.47$$

$$\text{Dc} = 4.5 \times 60.7 + 25 + 50 + 92.5 = 3.77$$

$$\text{Ed} = 4.5 \times 60.7 + 25 + 50 + 75 + 118.5 = 3.57$$

$$\begin{array}{cccccc} * & * & * & * & * & * \end{array}$$

LIVE LOAD STRESSES IN ANCHOR SPAN.

Chord Stresses.

Reaction when suspended and cantilever arms are fully loaded.

$$\begin{aligned}R &= -(\overline{100}^2 + 200 \times 100 + 100) - (100 + 200) + 50 \\ &= -6\end{aligned}$$

$$\text{Cos. } \alpha = .96293$$

The method of procedure used in the analysis of stresses for a simple truss may be applied here.

$$ab = -6 \times 25 + 24 = -6.25$$

$$BC = 6 \times 25 + 24 \times .963 = 6.50$$

$$bc = -6 \times 50 + 31 = -9.68$$

$$CD = 9.68 + .963 = 10.05$$

$$cd = -6 \times 75 + 38 = -11.84$$

$$DE = 11.84 + .963 = 12.2)$$

$$de = -6 \times 100 + 45 = *13.32$$

The effect of loading only the anchor span is the reversal of stresses in the upper and lower chord of same. The live load chord stresses under this condition are:-

$$ab = 1.5 \times 25 + 24 = 1.561$$

$$BC = -1.561 + .963 = -1.623$$

$$bc = 1.5 \times 50 - 25 + 31 = 1.612$$

$$CD = -1.612 + .963 = -1.68$$

$$cd = 1.5 \times 75 - 25 - 50 + 38 = .988$$

$$DE = -.988 + .963 = -10.26$$

$$de = 1.5 \times 100 - 25 - 50 - 75 + 45 = 0$$

Web Stresses in Anchor Span.

$$\text{Load at: - b} \quad R = \frac{3}{4}$$

$$c \quad R = I/2$$

$$d \quad R = I/4$$

$$\text{Rest of Bridge} \quad R = -6$$

$$aB \text{ (Min)} = -1.5 + .693 = -2.168$$

$$aB \text{ (Max)} = 6 + .693 = 8.67$$

$$Bb \text{ (Min)} = 1.5 \times 60.7 + 85.7 = 1.062$$

$$Bb \text{ (Max)} = -6 \times 60.7 + 85.7 = -4.284$$

$$Cb \text{ (Min)} = -.75 \times 60.7 + 66.8 = -.683$$

$$Cb \text{ (Max)} = 5.25 \times 60.7 + 85.7 + 66.8 = 6.07$$

$$Cc \text{ (Min)} = .75 \times 60.7 + 110.7 = .412$$

$$Cc \text{ (Max)} = -5.25 \times 60.7 - 85.7 + 110.7 = -3.66$$

$$Dd \text{ (Min)} = .25 \times 60.7 + 135.7 = .112$$

$$Dd \text{ (Max)} = -4.75 \times 60.7 + 85.7 + 110.7 + 135.7 \\ = -3.58$$

$$Ed \text{ (Min)} = 0$$

$$Ed \text{ (Max)} = 4.5 \times 60.7 + 85.7 + 110.35 + 135.7 + 118.5 \\ = 5.11$$

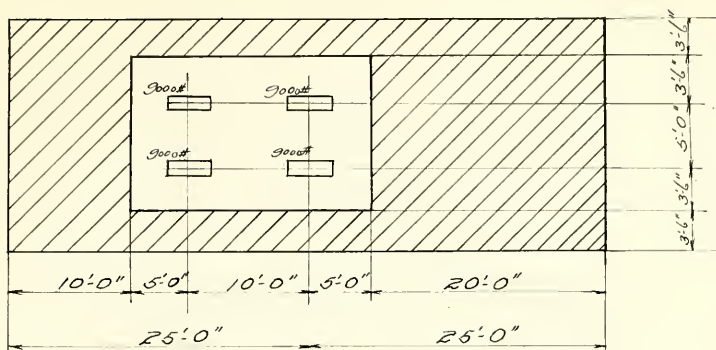
$$Ee \text{ (Min)} = -18 + 1 = -17$$

$$Ee \text{ (Max)} = -16 + 1 = -15$$

$$Cd \text{ (Min)} = .25 \times 60.7 + 92.5 = -.165$$

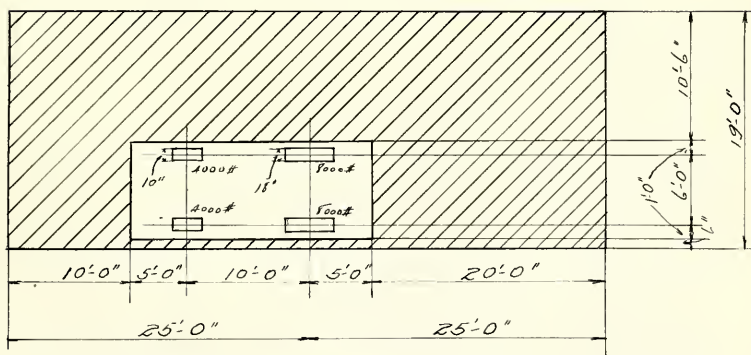
$$Cd \text{ (Max)} = 4.75 \times 60.7 + 85.7 + 110.7 + 92.5 = 5.25$$

STREET CAR AND UNIFORM LOAD



(Sketch #4)

12 TON-TRACTION ENGINE & UNIFORM-LOAD.



(Sketch #4a)

(10-10-10)

(10-10-10)

Planking:-

The total thickness of planking is to be 5.5 inches, 1.5 inches of this total to be wearing surface. This wearing surface is to be of oak and capable of being replaced. The thickness to resist bending then, will be 4 inches. The allowable stress for oak = 1200/sq.in.. The weight of planking is 4.5# per board foot. The specifications (Art. 18) state that stringers shall be spaced not farther in feet than the thickness in inches of the floor.

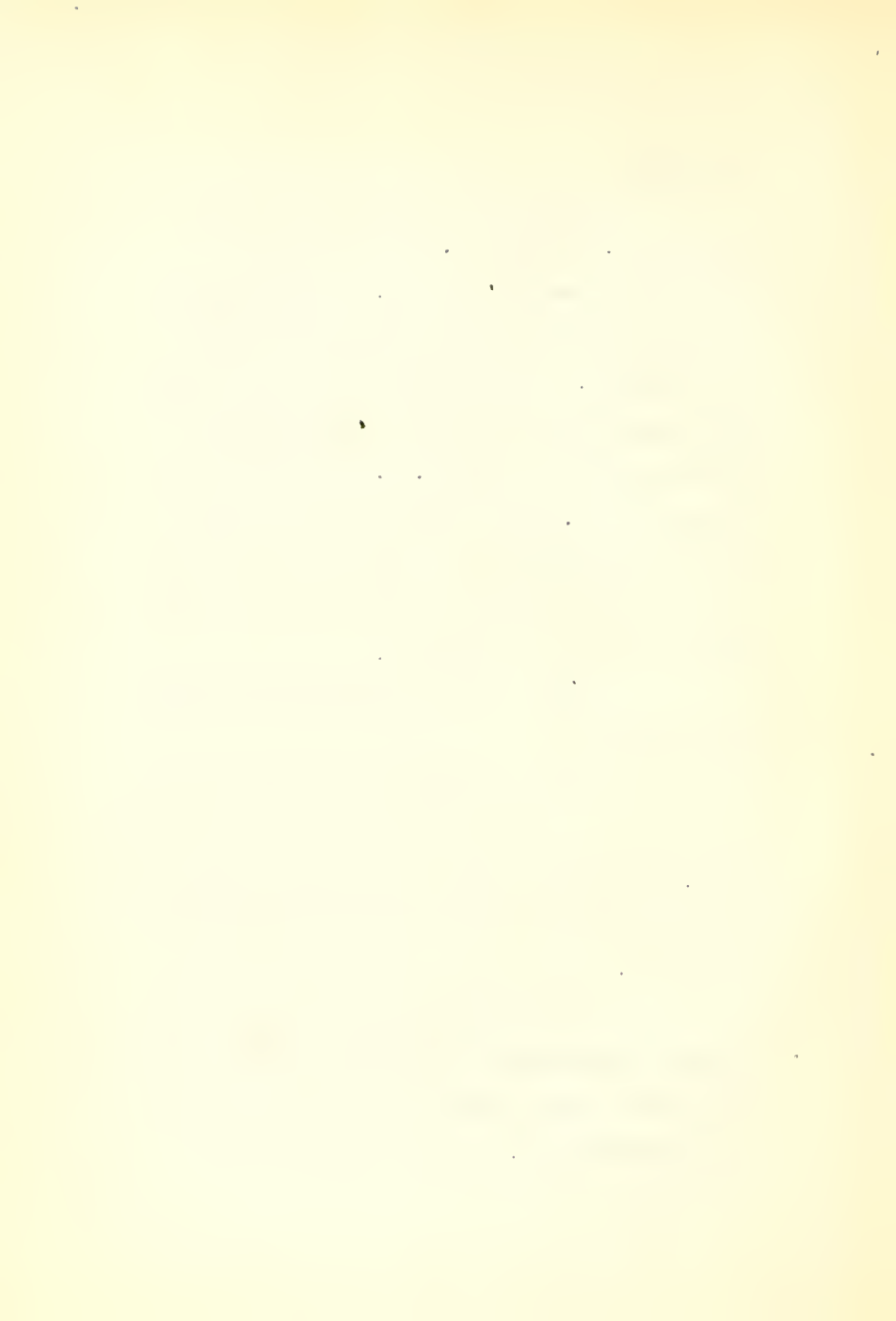
Let L = distance between two roadway stringers.

Let b = breadth of planking in in..

" d = depth of planking in inches.

Then, for maximum bending moment place one rear wheel of traction engine half way between two stringers.

The calculations from here on will be self-explanatory. We will endeavor to design the floor system so that it will represent a complete analysis.



$$\text{Resisting Moment} = SI/c = 1200bd + 6 = 38,400''\#$$

$$\text{Bending Moment} = 4000 \times L/2 - 4000 \times 4.5 =$$

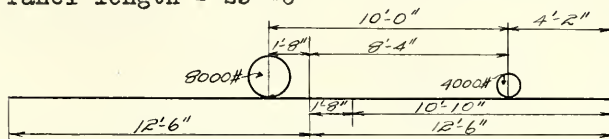
$$2000L - 1800 = 38,400$$

$$L = 28.2$$

In view of this analysis we will space stringers
2'-3" apart.

DESIGN OF ROADWAY STRINGERS.

$$\text{Panel length} = 25'-0''$$



$$\text{B. M.} = (8000 \times I4.17 + 4000 \times 4.17 + 25) I0.83 \times I2 =$$

$$678,000''\#$$

$$\text{For stringers use } I5'' \text{ I-Beam} = 42''\#$$

$$\text{Planking} = 5.5 \times 4.5 \times 2.25 = 55.7$$

$$\text{Total per Lin. Ft.} = 97.7''\#$$

Dead load bending moment=

$$97.7 \times 25 \times I2 + 8 = 91,500''\#$$

Bending Moment caused by wheel loading=678,000

$$\text{" " " " dead load} = 91,500$$

$$\text{Total} = 769,500''\#$$

$$I/c = 769,500 \div I3000 = 59.2$$

Section Modulus of a 15"-42# I-Beam=58.9

A 15"-42# I-Beam is O.K. but it is perhaps better design to use a 15"-45# I-Beam. S.C.=60.8

*** TRACK - STRINGERS ***

$$B.M. = (15 \times 9000 + 5 \times 9000 + 25) 10 \times 12 = 815,000 \text{"}\#$$

$$\text{Planking} = 5.5 \times 4.5 \times 2.5 = 62 \text{# per lin.ft.}$$

$$\text{Track Rails} = 30 \text{# " " "}$$

$$18 \text{"} \text{ I-Beam Stringer} = \underline{55 \text{#}} \text{ " " "}$$

$$\text{Total} \quad \quad \quad 147 \text{# " " "}$$

$$D.L.B.M. = w l^3 / 8 = 147 \times 25 \times 12 \div 8 = 139,000 \text{"}\#$$

$$\text{Bending Moment from the car wheel} = 815,000 \text{"}\#$$

$$\text{" " " dead load} = \underline{139,000 \text{"}\#}$$

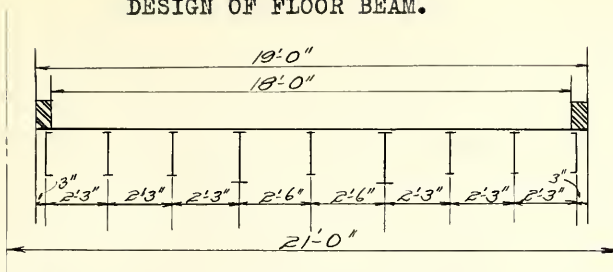
$$\text{Total} = 954,000 \text{"}\#$$

$$\frac{954,000}{13,000} = 73.5$$

The 18" 55# I-Beam assumed is O.K.

Its section modulus = 81.5

DESIGN OF FLOOR BEAM.



Weight of Planking = $5.5 \times 4.5 \times 25 \times 19 = 11,750$

Weight of Steel:-

2-15" Channels @ $33\# = 66\#$

5-15" I-Beams @ $45\# = 225\#$

2-18" I-Beams @ $55\# = 110\#$

2-90# Rails @ $30\# = 60\#$

Total = $461\#/\text{lin. ft.}$

Weight of the steel per panel:-

$461 \times 25 = 11,525$

Planking = $11,750\#$

Steel = $11,525\#$

Fl. Beam = $\frac{2,415\#}{(115 \times 21)^*}$

Total = $25,690\#$

D.L.B.M. = $25,690 \times 21 \times 12/8 = 810,000\#$

115# is the assumed weight of Floor Beam per

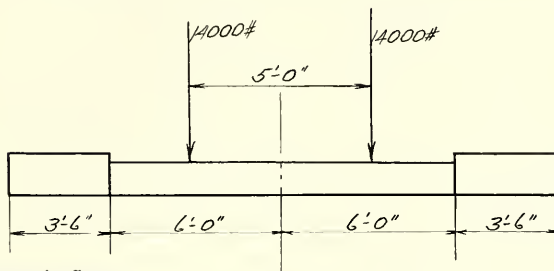
Lin. Ft.

Live Load Stresses for Floor Beam

There is a chance of for two kinds of loading.

1st.) Street car and uniform load.

2nd.) Traction engine and uniform load.



Street Car:-

Each wheel load = 9000#

Wheel load reaction = $9000 + 9000 \times 15 \div 25 = 14,400\#$

The uniform load reaction per foot of floor beam from loading ahead and behind street car = $10 \times 100 \times 5 + 20 \times 100 \times 15 = 1000\#$

On sides of car per Ft. of Fl. Beam =

$25 \times 100 = 2500\#$

Fl. Beam reaction = $3.5 \times 2500 = 8750$

$6 \times 1000 = \underline{6000}$

Total = $14750\#$

Street car load = $14,400\#$

Total reaction = $14,400 + 14,750 = 29,150\#$

Taking moments at center:-

$$M = 29150 \times 11.5 - 8750 \times 7.75 - 6000 \times 3 - 14400 \times 2.5 = 184262' \#$$

$$184,262' \# \times 12 = 2,211,144' \#$$

$$\text{Live load Moment} = 2,211,144$$

$$\text{Dead load Moment} = \underline{810,000}$$

$$\text{Total moment} = 3,021,144' \#$$

From this it may be noted that a built up section is required.

$$\text{Use 2Ls } 5 \times 3.5 \times 11/16 \quad \text{Area} = 10.74 \text{ sq.in.}$$

$$\text{For rivet holes deduct} \quad \underline{1.38} \quad " \quad "$$

$$\text{Net Area} = 9.46 \quad " \quad "$$

Web of floor beam taken as 24"

$$\text{Effective depth} = 24 - (2 \times 1.72) = 20.56"$$

Area of metal required:-

$$\frac{3,021,144}{13,000} = 9.2$$

The assumed section is hence O. K.

Weight of section per lin. ft. =

$$4\text{Ls } 5' \times 3.5' \times 11/16 @ 18.3 \# = 73.2$$

$$\text{Web Plate } 24' \times 1/2' = \underline{40.8}$$

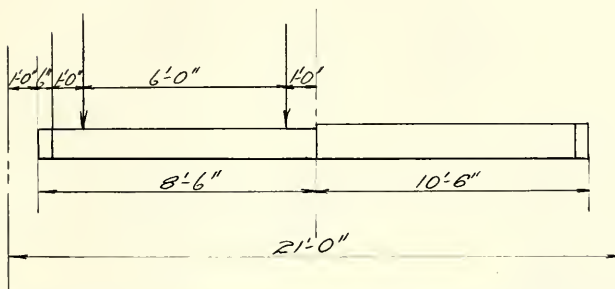
$$\text{Total} \quad 114.0 \#$$

Assumed section weight = 115# Hence O. K.

For investigating shear, the traction engine will be set against the wheel guard with the rear wheel on floor beam.

Traction engine assumed to cover a space

$$8' \times 20'$$



$$\text{Wheel load reaction} = 8000 + (4000 \times 15 + 25) =$$

$$10,400\#$$

Uniform load reaction going to floor beam from ahead and behind engine:-

$$= (10 \times 100 \times 5 + 20 \times 100 \times 15) + 25 = 1000\#$$

$$\text{Side of traction engine} = 25 \times 100 = 2500\#$$

$$R \times 2I = 8 \times 1000 \times 15.5 + 2500 \times 10.0 \times 6.5 +$$

$$10,400(17.5 + 12.5) = 598,500$$

Street car loading the gives 29,150 # for reaction of floor beam.

Maximum Stringer Reactions .

Roadway Stringer:-

$$\text{Reaction} = 8000 + (4000 \times 15 + 10 \times 100 \times 2.5 \times 5 + 25) = 10900$$

Tr. Stringer:-

$$\text{Reaction} = 9000 + (9000 \times 15 + 10 \times 100 \times 2.5 \times 5 + 25) = 14900$$

$$\text{Planking} = 5.5 \times 4.5 \times 2.25 = 55.7$$

$$\text{Roadway Stringer} \quad \underline{42.0}$$

$$\text{Total} = 97.7$$

Again:-

$$\text{Planking} = 5.5 \times 4.5 \times 2.5 = 62$$

$$\text{Track Stringer} = 55$$

$$\text{Rail} = 30$$

147# Total

$$\text{Dead Load} = 98 \times 25 / 2 = 1225 \quad (\text{Roadway Stringer})$$

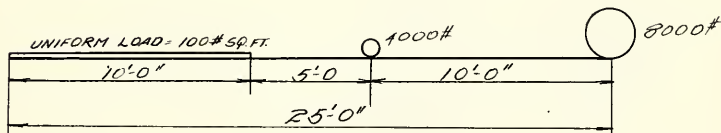
$$\text{" " " } = 147 \times 25 / 2 = 1838 \quad (\text{Track Stringer})$$

Total reaction of track Stringer=

$$14,900 + 1838 = 16,738\#$$

Total reaction of Roadway Stringer=

$$10,400 + 1,225 = 11,625\#$$



LOADS FOR TRUSSES

Live Load:-

See table A of Cooper's Spec. P.10
Class C Loading.

L. L. 1000# per ft. of car track.

60# per sq. ft. of remaining surface.

Loading per panel per truss:-

$$1000 \times 25 / 2 = 12,500\#$$

$$\text{Also } 60 \times 25 / 2 \times (19 - 12) = \underline{5,250\#}$$

$$\text{Total} = 17,750\#$$

Consider then the live load panel load as
equal to 18,000#

* * * * *

A DETERMINATION OF THE DEAD LOAD PANEL
WEIGHT PER TRUSS WILL BE MADE: these weights
will be determined from a series of formulas.
Certain weights however are known and they are

Planking per panel per truss:-

$$25 \times 9.5 \times 5.5 \times 4.5 = 5569\#$$

$$\text{Wheelguards:- } 25 \times 48 \times 4.5 + 12 = 450\#$$

$$\text{Rails:-} = \underline{750\#}$$

$$\text{Total} = 6769\#$$

Steel in Floor:- 11.5ft. @ 115#	= 1208
2.5x25x45	= 2813
1.0x25x33	= 825
1.0x25x55	= <u>1375</u>
Total	= 6241
Connections	= <u>250</u>
Grand Total	= 6490

Call it 6500#

$$6800 + 6500 = 13,300 \text{ or } 532\# \text{ per. lin.ft.}$$

* * * * *

FORMULA FOR WEIGHT OF BRIDGE BY E. S. SHAW.

$$w = 300 + I + 22b + I/15b(1 + .0011)$$

w = weight of steel per lin. ft. of span.

l = length of span i feet.

b = breadth of roadway including sidewalk.

Note:- This formula does not include weight of wooden floor, but assumes the weight at 10# per sq. ft. of floor surface. The weight of the wooden floor in our case has been figured exactly.

$$w = 300 + 200 + 22 \times 19 + 1/15 \times 19 \times 200(1 + .001 \times 200) = 1,222$$

$$\frac{1222}{2} = 611\# \text{ per. lin. ft.}$$

$$611 \times 25 = 15275 \# = \text{Wt. per panel per truss.}$$

$$15,275 + 6,800 + 750(\text{Fence}) = 22,825.$$

This is the dead load panel weight from Shaw's formula.

* * * * *

WADDEL'S FORMULA.

$$w = 34 + 22b + 0.16bl + 0.7l$$

$$= 34 + 418 + 608 + 140 = 1200 \#$$

w = Total dead load in #s per lin. ft. of bridge including flooring, stringers, trusses side-walks and laterals.

l = span in feet.

b = clear width of roadway sidewalk.

$$1200 \div 2 = 600 \# \text{ per lin. ft. of truss.}$$

$$600 \times 25 = 15000 \# \text{ dead load panel weight.}$$

* * * * *

FROM KETCHUM'S DESIGN OF HIGHWAY BRIDGES.

From the curves, weight of steel in bridge exclusive of fence = 75000# From previous data then our panel load becomes = to 13,000#

This however is for the lightest kind of a highway bridge, and will be neglected here.

From another set of curves in Ketchum's Design of Highway Bridges we get a panel weight totaling 20,000#

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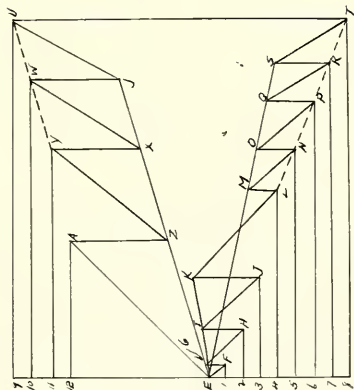
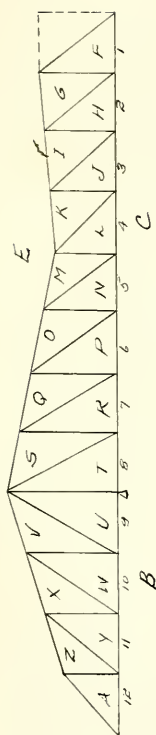
Making the necessary substitutions in formula given by H. G. Tyrrel we get a panel load of 17,000#

From data obtained from the American Bridge Company, a 200'-0" span through bridge actually up has its two trusses weighing 72,000#. The loading for which the bridge was designed was called Class C.

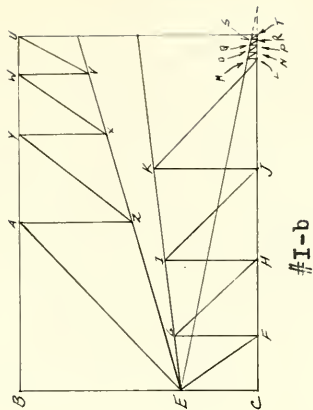
Using this data panel load becomes

19,000 #

It appears that from the loading we have assumed that our floor system is very heavy. This therefor increases the dead load. From preliminary trials of sections it has been found that 23,000# per panel would be about the right assumption. This was the result obtained from Shaw's formula.



#I-a



#I-b

PLATES #8 I-a & I-b.

EXPLANATION OF PLATES #I-a & #I-b?

Plate #I-a is the graphical solution for the stresses due to dead load of the cantilever bridge during erection. A panel load of unity is considered concentrated at each panel point. There is no need of describing the method of procedure since in drawing the plate no difficulties of any importance arise.

* * * * * *

Plate #I-b is the graphical analysis of the stresses in the members of the cantilever bridge due to the live load of erection. For this, a panel load of unity is considered as concentrated at m. For reasons above stated the method of procedure will not be explained.

* * * * * *

The stresses are tabulated on page ____
The panel load of unity may be considered as one Kip, and therefore the coefficient of the table multiplied by the real panel load will give the stress in the member.



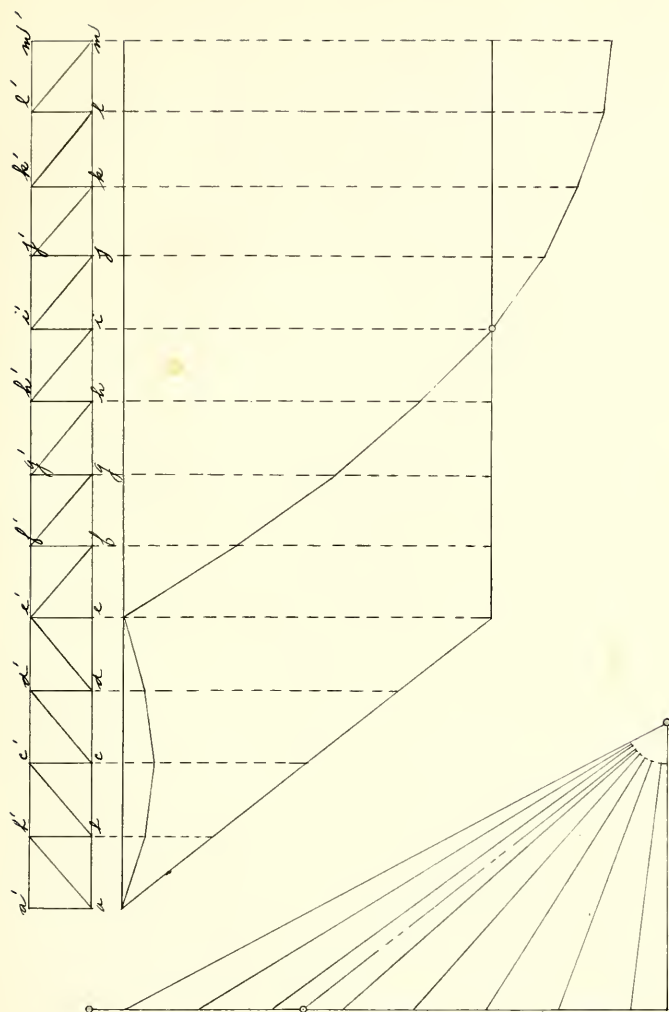


PLATE #2

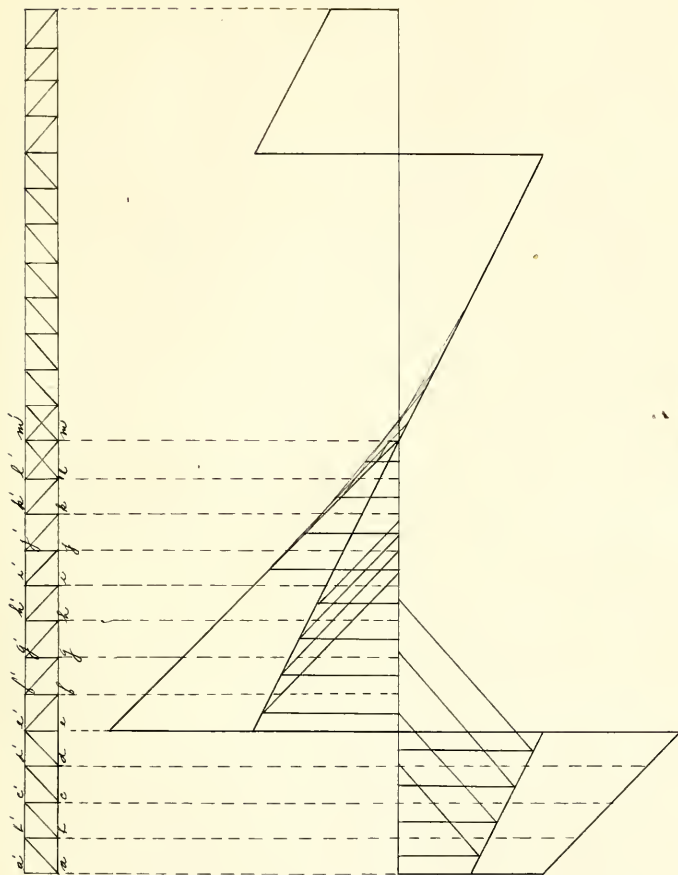


PLATE #3



12	N	X	11	M	W	10	L	V	9	K	J	8	H	I	7	G	U	6	F	T	5	E	S	4	D	R	3	C	Q	2	B	P	1	A	O
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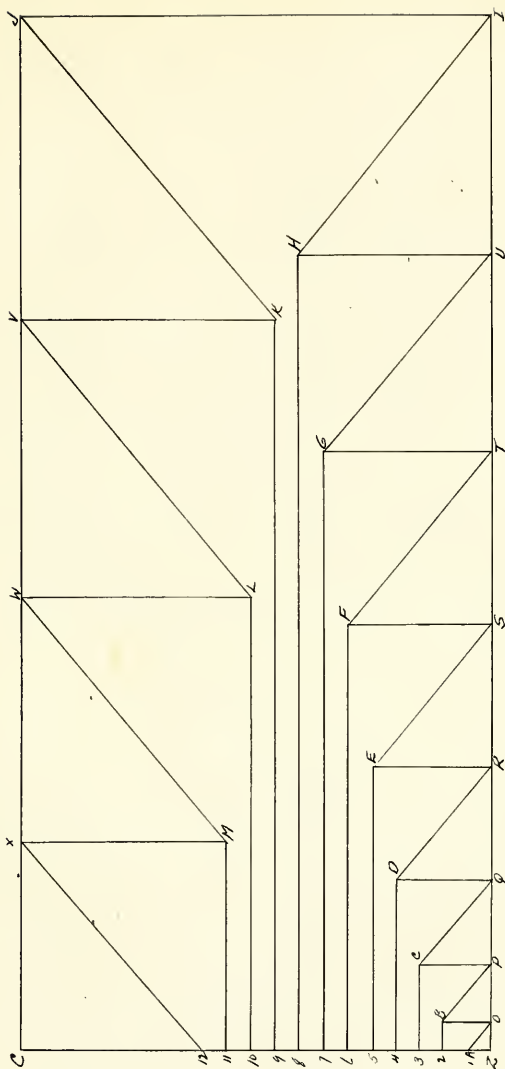


PLATE #4.

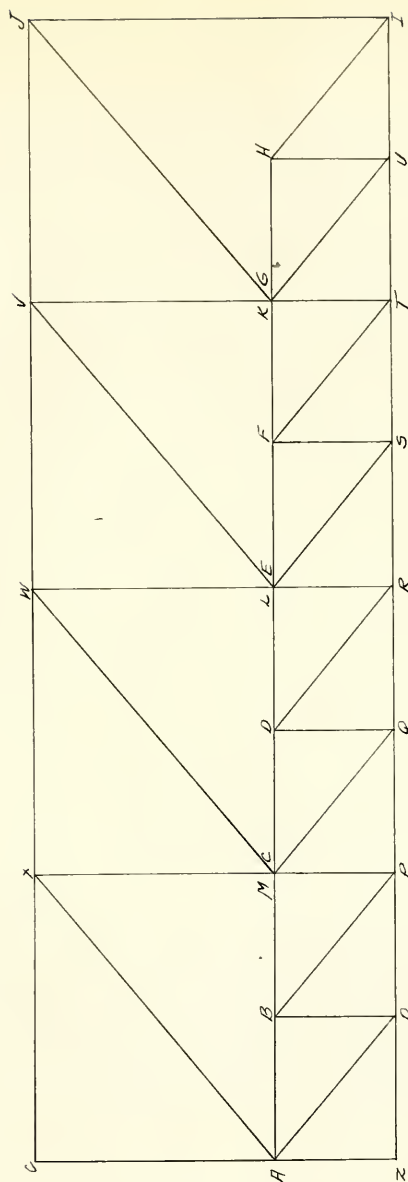
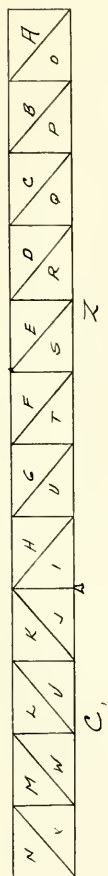


PLATE #5.

EXPLANATION OF PLATES #2 and #3.

It is very necessary that the lateral forces exerted on a bridge be considered. The stresses in the lateral systems of this cantilever bridge will therefore be accurately determined. Art. 39 of Cooper's Specifications says "To provide for wind and vibrations, the top lateral bracing in deck bridges, and the bottom lateral bracing in through bridges, shall be proportioned to resist a lateral force of 300# for each foot of span, 150# Of this to be treated as a moving load. The bottom lateral bracing in deck bridges and the top lateral bracing in through bridges, shall be proportioned to resist a lateral force of 150# per lineal foot. " The determination of stresses in the laterals due to these forces may be solved by graphics in the usual manner.

Plates #2 & #3 are the graphical solution of the stresses in the lateral system after the bridge is in place considering a lateral force of one Kip at each panel point. Strictly speaking

this system is a continuous truss and should be analysed as such. Owing to the complications that arise in solving such a problem it was thought best to consider the system as a cantilever with zero B. M. at I.

Plate"#2" then gives the stresses due to bending moment in the chord members. Plate"#3" gives the stresses in the web members due to shear. In drawing-up theses plates a panel load of one Kip (stated before) was considered. The coefficient then that is obtained multiplied by 3.75 gives the stress in the respective member. By making the assumption stated above the problem reduces to a very simple one.

Plate #4 represents a stress diagram due to the lateral forces during erection.

Plate #5 represents the stress diagram considering a panel load of unity concentrated at the end of the bridge while in erection. Such a loading could perhaps never occur the object having been to compare the drawing with that of Plate #I-b. This truss having parallel chords.

TABLE #I

	BRIDGE UP				BRIDGE IN ERECTION.-				WIND	
	Dead Load		Live Load		Dead Load		Live Load			
J	+	-	+	-	+	-	+	-	+Or -	+Or -
aB	6.50		8.67	2.17	5.40		1.40			
bC	4.87		6.50	1.62	8.09		2.20		19.05	11.90
cD	8.38		10.05	1.68	13.38		3.34		30.38	19.65
dE	11.92		12.30	1.03	17.40		4.08		42.80	28.60
eF	10.63		10.63		18.02		4.50		42.80	28.60
fG	7.40		7.40		15.70		4.45		33.30	19.65
gH	3.90		3.90		13.15		4.37		25.00	11.90
hI	0		0		10.70		4.26		17.85	5.36
iJ		3.26		3.26	5.60		2.80		11.90	0
jK		5.04		5.04	2.44		1.67		7.14	4.16
kL		5.23		5.23	.78		.76		3.57	7.15
lM		6.06		6.06	0		0		1.19	8.93

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TABLE #2.

	BRIDGE UP				BRIDGE IN ERECTION.				WIND.	
	Dead Load		Live Load		Dead Load		Live Load			
	+	-	+	-	+	-	+	-	+or -	+or -
ab		4.69	1.56	6.25		7.80		2.10	8.91	5.36
bc		8.06	1.61	9.68		12.90		3.20	19.05	11.90
od		18.06	.99	11.84		16.76		3.94	30.38	19.65
de & ef		13.32	0	13.32		20.00		4.44	42.8	28.60
fg		10.40		10.40		17.60		4.40	33.30	19.65
gh		7.25		7.25		15.20		4.35	25.00	11.90
hi		3.85		3.85		12.82		4.27	17.85	5.36
ij	0	0	0	0		10.42		4.16	11.90	0
jk	3.24		3.24			5.55		2.77	7.14	4.16
kl	5.00		5.00			2.50		1.66	3.57	7.15
lm	5.69		5.69			.75		.75	1.19	8.93

TABLE #3

	BRIDGE UP.				BRIDGE IN ERECTION.			
	Dead Load		Live Load		Dead Load		Live Load	
	+	-	+	-	+	-	+	-
bC	4.5		6.07	.683	8.20		1.80	
cD	3.77		5.25	.165	7.20		1.30	
dE	3.57		5.11	0	6.72		1.02	
Ef	6.09		6.09		4.90		.08	
Fg	5.88		5.88		4.50		.10	
Gh	5.84		5.84		4.10		.13	
H1	5.92		5.92		3.70		.15	
Ij	4.5		4.5		6.80		1.93	
Jk	2.59		2.80		4.50		1.64	
Kl	1.06		1.78		2.75		1.42	
Lm	.63		1.57		1.25		1.26	
Mn			.94					

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TABLE #4.

	BRIDGE UP.			BRIDGE IN ERECTION.			
	Dead Load.		Live Load	Dead Load		Live Load.	
	+	-	+	-	+	-	+
Bb		3.19	1.06	4.25	5.40		140
Cc		2.70	.41	3.68	5.00		1.10
Dd		2.57	.11	3.58	4.95		0.90
Ee		15.00		15.00	16.50		3.00
Ff		4.32		4.32	3.30		.08
Gg		4.00		4.0	2.80		.09
Hh		3.70		3.70	2.30		.10
Ii		3.50		3.50	1.80		.12
Jj		2.11		2.33	3.70		1.33
Kk		.90		1.5	2.32		1.20
Ll	1.82			.91	1.05		1.1
Mm	0			.75	0		.79

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TABLE #5.

	BRIDGE UP			BRIDGE IN ERECTION				Maximum.
	Dead Load		Live Load	Dead Load		Live Load		
	+	-	+	+	-	+	-	
Ii		70,000			25,200		26,000	-196,000
Jj		42,200			50,400		26,600	-126,100
Kk		18,000			32,200		24,000	-72,000
Ll	3,640				14,700		22,000	+3,640 -36,700
Mm	0				0		0	-27,000
Ij	90,000		162,000	94,400		38,600		252,000
Jk	51,800		103,000	63,000		32,800		154,800
Kl	21,280		64,100	38,500		28,400		85,380
Im	12,560		56,500	18,200		25,200		69,060
Ij		65,200		117,400	78,500		56,000	+134,500 -182,600
JK		100,800		182,000	35,700		33,400	+69,100 -282,800
KL		114,600		212,600	11,200		15,200	+26,400 -327,200

TABLE #5-Cont'd.

	BRIDGE UP			BRIDGE IN ERECTION			Maximum.
	Dead Load		Live Load	Dead Load		Live Load	
	+	-	+	+	-	+	
LM		121,200		218,100	0	0	-339,300
lj	0		0		147,000	83,200	-230,200
jk	64,800		116,700		78,500	55,400	+181,500
kl	100,000		180,000		35,000	33,200	-133,900
lm	113,000		204,900		10,500	15,000	+280,000
Mn			33,820				-68,200
ML			33,820				+318,700
							-25,500
							33,820
							33,820

TABLE #6.

	+	+		-	-
ab	8.91	5.36	a'b'	0	0
bc	19.05	11.90	b'c'	8.91	5.36
cd	30.38	19.65	c'd'	19.05	11.90
de	42.80	28.60	d'e'	30.38	19.65
ef	42.80	28.60	e'f'	33.30	19.65
fg	33.30	19.65	f'g'	25.00	11.90
gh	25.00	11.90	g'h'	17.85	5.36
hi	17.85	5.36	h' i'	11.90	0
ij	11.90	0	i'j'	7.14	4.16
jk	7.14	4.16	j'k'	3.57	7.15
kl	3.57	7.15	k'l'	1.19	8.93
lm	1.19	8.93	l'm')0	9.52
ab'	11.67	7.00	aa'	7.50	4.50
bc'	13.20	8.55	bb'	8.50	5.50
cd'	14.75	11.10	cc'	9.50	6.50
de'	16.35	11.65	dd'	10.50	7.50
fe'	12.43	11.65	ee'	19.50m	15.00
gf'	10.90	10.10	ff'	8.00	7.50
hg'	9.33	8.55	gg'	7.00	6.50
ih'	7.75	7.00	hh'	6.00	5.50
jh'	6.22	5.44	ii'	5.00	4.50
kj'	4.66	3.79	jj'	4.00	3.50

TABLE #7.

METAL IN SUSPENDED SPAN.				
	Member	Section.	Length	Weight.
2	IJ	2 Channels 15"-35#	25.18	3525
2	JK	" " " "	25.18	3525
2	KL	" " " "	25.18	3525
2	LM	" " 15"-40#	25.00	4000
2	ij	" " 12"-25#	25.00	2500
2	jk	" " " "	25.00	2500
2	kl	" " 12"-30#	25.00	3000
2	lm	" " " "	25.00	3000
2	Ij	" " 12"-25#	34.65	3465
2	Jk	" " 10"-20#	36.80	2944
2	Kl	" " " "	39.10	3128
2	Lm	" " " "	41.50	3320
2	Ii	" " 12"-25#	24.00	2400
2	Jj	" " 10"-20#	27.00	2360
2	Kk	" " 10"-15#	30.00	1800
2	Ll	" " " "	33.00	1980
I	Mm	" " " "	33.00	990
Total:-			47962#	

TABLE #8.

METAL IN CANTILEVER & ANCHOR ARMS.				
2	aB	2 Channels I5"-40#	34.80	5568
2	BC	" " I5"-45#	25.95	4671
2	CD	" " I5"-55#	25.95	5709
2	DE	" " " "	25.95	5709
2	EF	" " " "	25.55	5620
2	FG	" " " "	25.25	5620
2	GH	" " I5"-45#	25.55	4599
2	HI	" " I5"-33#	25.55	3373
2	ab	" " I2"-30#	25.00	3000
2	bc	" " " "	25.00	3000
2	cd	" " I2"-35#	25.00	3500
2	de	" " " "	25.00	3500
2	ef	" " " "	25.00	3500
2	fg	" " " "	25.00	3500
2	gh	" " I2"-30#	25.00	3000
2	hi	" " " "	25.00	3000
Total.				66869#

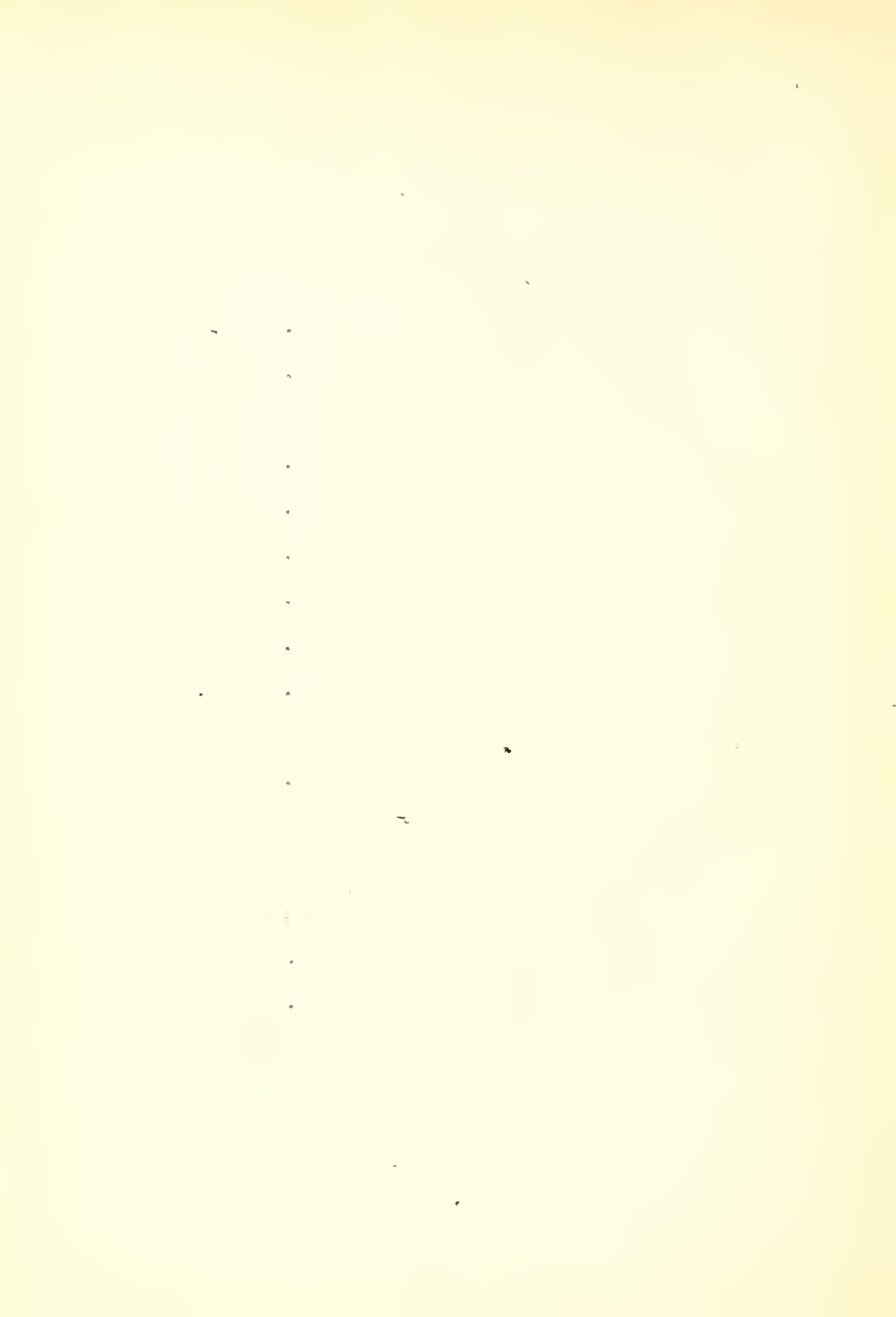


TABLE #8 Cont'd.

METAL IN CANTILEVER & ANCHOR ARMS.				
2	bC	2 Channels 12"-30#	39.90	4788
2	cD	2 Channels " "	45.50	5460
2	dE	" " " "	51.50	6180
2	Ef	" " " "	51.50	6180
2	Fg	" " " "	47.00	5640
2	Gh	" " " "	42.60	5112
2	Hi	" " " "	38.50	4620
2	Bb	" " 12"-25#	24.00	2400
2	Cc	" " " "	31.00	3100
2	Dd	" " " "	38.00	3800
2	Ff	" " " "	39.75	3975
2	Gg	" " " "	34.50	3450
2	Hh	" " " "	29.25	2975
Total				57680#

FIGURING PANEL WEIGHTS.

From Table #7 the weight of sections is 47,962# This of course excludes the details. For this a percentage of 40% is to be added. The panel weight of the suspended span $= (47,962 + 8 + 40\%) + 14000 = 22,393\#$ This agrees very closely with the panel weight assumed.

For the cantilever and anchor spans the total weight of steel in sections = $((135698 + 40\%) + 16) + 14000 = 26,000\#$ This was the panel weight used in designing members of cantilever and anchor arms.

14000 is a constant throughout each panel of the bridge, it being the weight of the floor system.

The 40% which was added for details was obtained from sets of figures for bridges actually in place. In tentatively designing a member complete it was found that the details very closely checked this figure.

- USE OF TABLES.-

The stresses due to live & dead load when bridge is in place are obtained by multiplying the coefficient of a member (Tables #1,2,3,&4) by its respective D. L. or I. L. panel weight. Thus to obtain the live load stress in the member K1 (taken at random) we find its coefficient in table #3 and multiply it by the Live Load Panel weight, viz:-

$$1.78 \times 18000 = 32,040\#$$

This reduced to an equivalent D. L. bases =
 $2 \times 32,040 = 64,080\#$ This stress is recorded in table #5.

Similarly the D. L. & I. L. erection stresses are respectively

$$2.75 \times 14000 = 38,500\# \text{ and}$$

$$1.42 \times 20,000 = 28,400\#$$

The stresses which occur when bridge is up do not occur while bridge is in erection. Then

$$21,280 + 64,080 = 85,360\# \text{ or Max. Stress.}$$

and this is recorded in column #II of Table #5

For this stress the member is designed.

Designing of Members.

Designing members offers no special difficulties. For that reason the calculations pertaining to the design of sections have been omitted. We do however submit the design of the Post Ee showing how we obtained the section. In a similar manner all members were designed.

Maximum stress in the post Ee occurs when there is a maximum reaction at the pier. This maximum reaction takes place when there is a full live load on the bridge.

Coefficient for D. L. = 15

Coefficient for L. L. = 15

Dead Load panel load in suspended span =

23,000#

Dead Load panel load in cantilever and

anchor spans = 36,000#

Live load panel load throughout bridge=

18,000#

$$\text{Stress in } E_e = (I5 \times 72,000) - 7 \times I6,000 =$$

$$968,000 \frac{\#}{\text{sq. in.}}$$

An approximate $r = 7.3$

$$\text{Area required} = 968,000 \div I3,400 = 72.25 \text{ sq. in.}$$

$$(P = 20,000 - (90 \times 45 \times I2 \div 7.3) = I3,400 \#)$$

Section to be tried.

$$2 \text{ Pls. } I9" \times 3/8" = I4.24 \text{ sq. in.}$$

$$4 \text{ Ls } 4" \times 4" \times II/I6" = 20.12$$

$$2 \text{ Pls. } 20" \times II/I6" = 27.52$$

$$2 \text{ Pls. } II" \times I/2" = \underline{II.00}$$

$$\text{Total} = 72.88 \text{ sq. in.}$$

To find r then

$$I/I2 \times I9 \times 3.375 + 7.12 \times 9.875 = 695$$

$$2 \times 7.17 + I0.06 \times (8.375) = 715$$

$$I/I2 \times II/I6 \times (20) = 458$$

$$I/I2 \times I/2 \times (II) = \underline{56}$$

$$\text{Total.} \quad I924$$

$$I924 \times 2 = 3848$$

$$r = 7.28$$

From this it is noted that assumed section is O. K.

CONCLUDING REMARKS.

The stresses due to wind have been omitted in designing the members for under specifications we are allowed to do so. They exceed nowhere 30% the maximum stains due to the dead and live loads upon a member. Regarding the design of portals it may be stated that they were considered as part of the "details" for which a percentage was allowed. This being 40%.

As the bridge now stands the hinge is at i in the unloaded chord. The same could have been placed at I of the "loaded" chord putting in the member iJ. By using this member the post Ii becomes zero and Ij drops out. Furthermore IJ and HI become = to zero. The member ij takes then a stress = to $3.5 \times 25 \div 27 = 3.24$, (Coefficient) for both dead and live load. $3.5 \div .73373 = 4.775$ (Coefficient) stress in iJ (Post) . One Kip equal the stress in Jj.

All other stresses throughout the bridge remain unchanged.

* * * * *

The reason for putting the hinge in the upper chord may be explained by stating that the appearance of the bridge was considered. By so doing a more pleasing outline for the structure being obtained.

*** A BIBLIOGRAPHY ***

on

CANTILEVER BRIDGES.

1) Adams, Henry

Designing wrought and cast iron structures.

1883 - 1887.

2) American Bridge company of New York.

Illustrations of a few typical railway and
highway bridges built by the company. 1908.

3) Balet, J. W.

Analysis of elastic arches, three hinged,
two hinged and hingeless of steel, masonry &
reinforced concrete. 1908.

4) Bender, Charles

Practical treatise on the properties of
continuous bridges. 1876.

5) Bovey, H. T.

Theory of structures. 1893.

6) Burr & Falk.

Graphic method by influence lines for
bridge and roof computations. 1905.

7) Burr & Falk.

Design and constuction of metalic bridges.

I905.

8) Burr, W. H.

Suspension bridges, arch ribs & cantilevers.

I9I3.

9) Heller, A. H.

Stresses in structures and accompanying
deformations. I908.

I0) Johnson, J.B., Bryan, & Turneaure.

Theory and practice of modern framed
structures. I9IO- II.

II) Ketchum, M. S.

Design of highway bridges and calculation
of stresses in bridge trusses. I908.

I2) Marburg, Edgar.

Framed structures and girders. I9II

I3) Merriam & Jacoby

Text book on roofs and bridges. I9II

I4) Moliter, D. A.

Kinetic theory of engineering structures
dealing with stresses deformation and work.
I9II.

I5) Skinner, F.W.

Types and details of bridge construction.

I904-06.

I6) Thompson, W. C.

Design of typical steel railway bridges.

I908.

I7) Tyrrell, H. G.

Artistic bridge design. I9I2

I8) Tyrrell, H. G.

History of bridge engineering. I9II.

I9) Waddell, J. A. L.

De pontibus. I903

20) Waddell, J. A. L.

Designing of ordinary highway bridges.

I894.

2I) Wells, M. B.

Steel bridge designing. I9I3.

22) Wright, C. H.

Designing of draw spans.

These books may be obtained in the library
of the Armour Institute of Technology.

* * * * *

PERIODICAL REFERENCES.

Cantilever Bridges.

- 1) Pittsburg and Lake Erie R. R. catilever bridge over
 the Ohio River at Beaver, Pa.
 * Amer. Soc. Civ. Eng. Proceedings. Jan. 1911.
- 2) Sewickly cantilever bridge over the Ohio River.
 * Amer. Soc. Civ. Eng. Proceedings. Sept. 1912.
- 3) Transport across Sydney Harbor.
 * Engineering. Nov.19th.1909.
- 4) A comparative study of limiting span, Maximum span
 and economic span for suspension bridges and canti-
 lever bridges.
 * Engineering & Contracting. May.7th. 1913.
- 5) Pittsburgh & Lake Erie cantilever bridge over the
 Ohio River at Beaver, Pa.
 * Engineering News Jan. 26th. 1911.
- 6) Sewickley cantilever bridge .
 * Engineering News. Feb.27th. 1913.
- 7) Reiforcing an old cantilever bridge, Phil. Pa.
 * Engineering News. Sept. 11, 1913.

- 8) Main Street bridge over the Buffalo Belt Line.
* Engineering Record Aug. 22nd. 1910.
- 9) Pittsburgh & Lake Erie cantilever bridge over the
Ohio River at Beaver, Pa.
* Engineering Record. Jan. 28th. 1911
- 10) The Beaver bridge main post and rocket bearing.
* Engineering Record Feb. 25th. 1911.
- 11) The bottom chords of the Beaver bridge.
* Engineering Record Mar. 11th. 1911.
- 12) Truss members of the beaver bridge.
* Engineering Record Mar. 25th. 1911.
- 13) Anchor pier bearings and typical connections,
Beaver bridge.
* Engineering Record. Apr. 22nd. 1911.
- 14) Suspended span of the Beaver bridge.
* Engineering Record. May 6th. 1911.
- 15) The expansion connection of the Beaver bridge.
* Engineering Record. May. 20th. 1911.

- 16) Arroya del Chico bridge.
* Engineering Record. July 29th. 1911.
- 17) Construction of the Kuskulana River bridge, Alaska.
* Engineering Record. Aug. 12th. 1911.
- 18) Through hand-plate girder span of the Susquehanna River bridge.
* Engineering Record. Apr. 20th. 1912.
- 19) Sewickley bridge across the Ohio.
* Engineering Record. Oct. 5th. 1912.
- 20) Suspension bridges and cantilevers (Serial)
Engineering Record. May. 17th. 1913.
- 21) Sewickley bridge over the Ohio.
* Génie Civil. Aug. 2nd. 1913.
- 22) Cantilever Bridge built by Siwash Indians.
* Railway and Engineering Review. Mar. 16, 1912.
- 23) Great bridge over the Red River in Indo China.
* Scientific American Supplement. Feb. 5th. 1910.

The sign, *, indicates that the article is illustrated.



